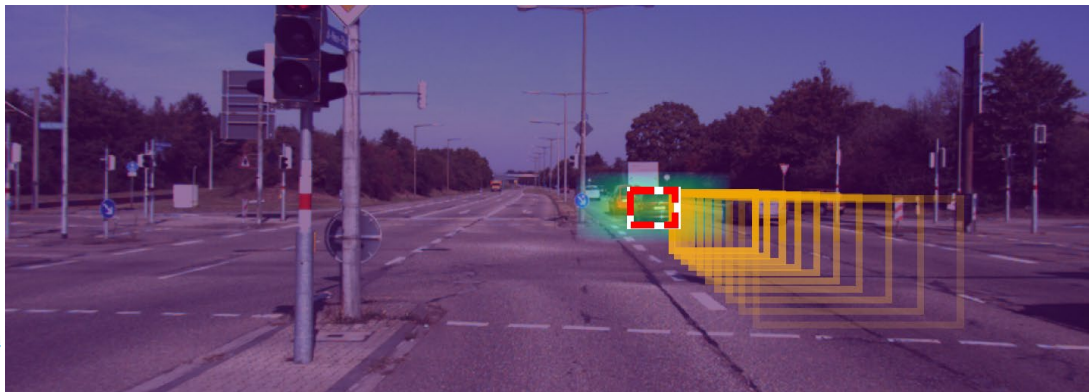


Robust Aleatoric Modeling for Future Vehicle Localization



THE UNIVERSITY
of NORTH CAROLINA
at CHAPEL HILL



6/17/2019

Max Hudnell

True Prie

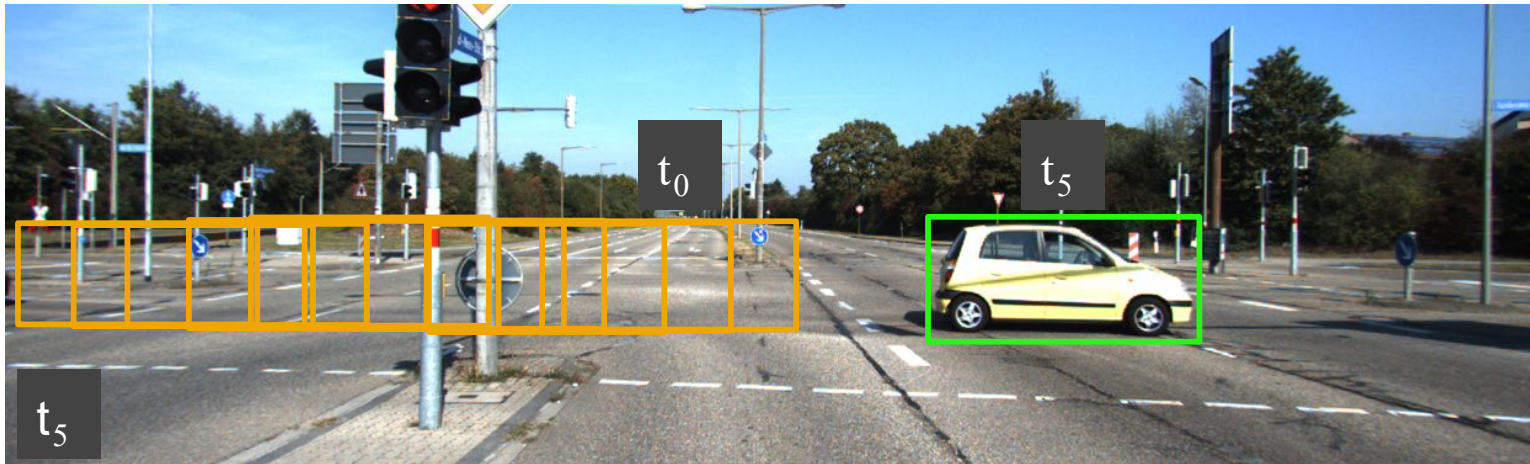
Jan Michael Frahm



UNC-CS

The Task

- What is (2D) future vehicle localization?
 - Localization – location and scale of object
 - => predicting where a vehicle is going to be



Our Goal

1. Predict where an object is likely to be
2. Produce an uncertainty estimate for our prediction



Related Work

- *W. Choi et al.* – Near-Online Multi-target Tracking with Aggregated Local Flow Descriptor
- *Dueholm et al.* – Trajectories and Maneuvers of Surrounding Vehicles with Panoramic Camera Arrays

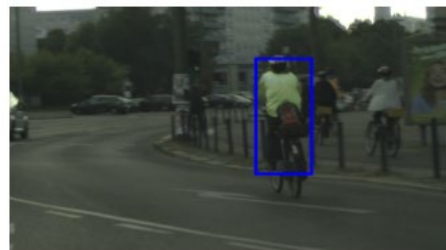
- Object tracking
- Utilize bounding box predictions
 - Linear and quadratic



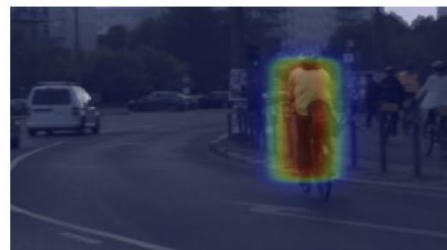
Related Work

Long-Term On-Board Prediction of People in Traffic Scenes under Uncertainty

- A. Bhattacharyya *et al.*, CVPR 2018
- RNN
- Gaussian uncertainty

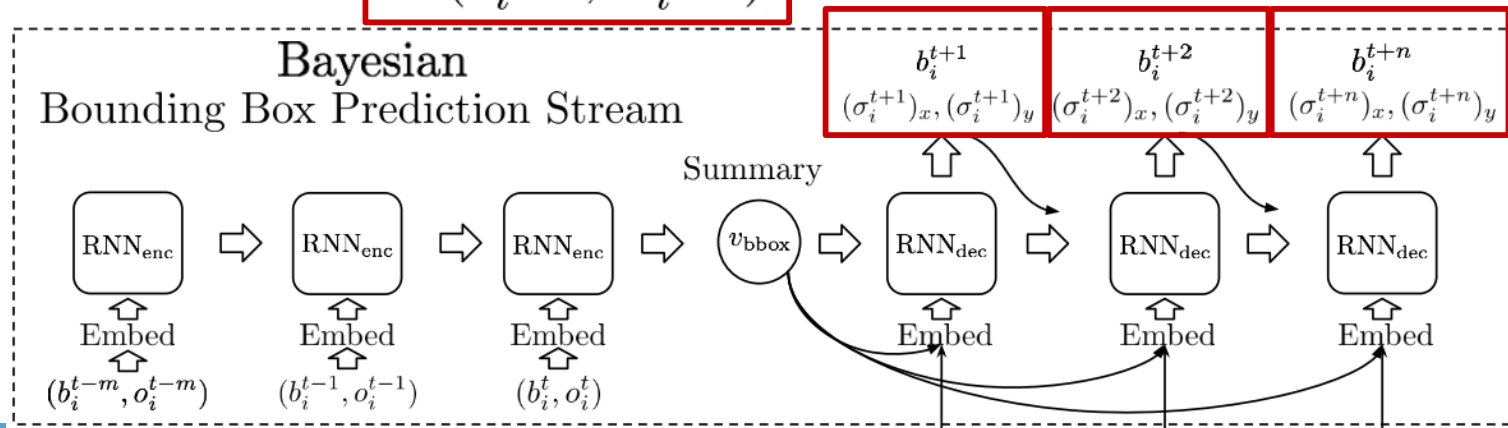


Last Observation: t



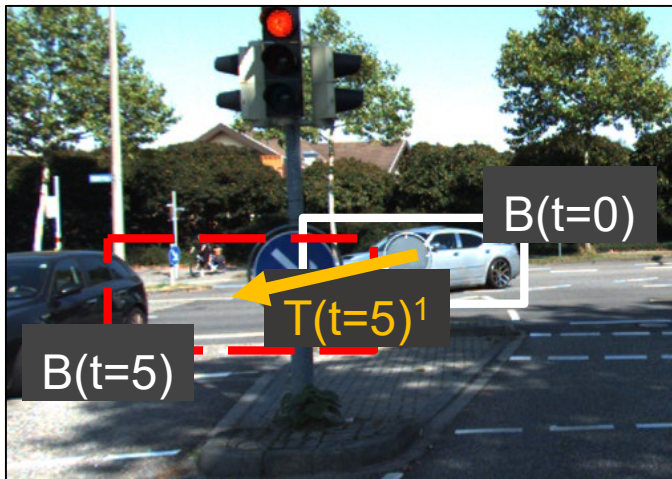
Prediction: $t + 5$

$$\mathcal{N}(b_i^{t+n}, \Sigma_i^{t+n})$$



Method

$$B_i = [x_i, y_i, w_i, h_i]$$



$$\mathbf{B} = \{B_{-n+1}, B_{-n+2}, \dots, B_0\}$$

Input layer (size=4n)

Output layer

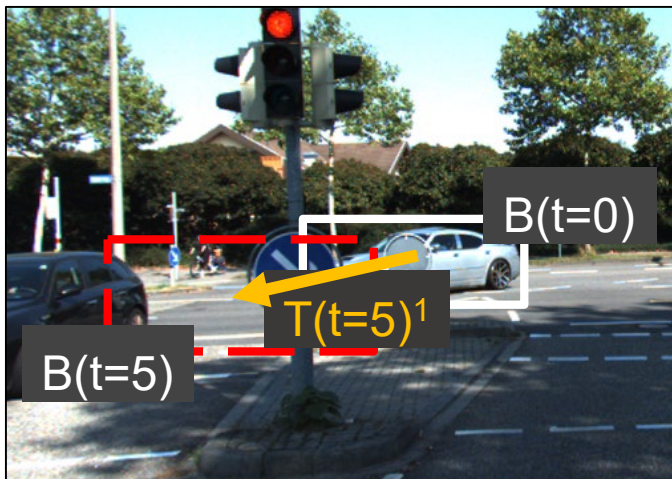
$$T(t) = [T_x(t), T_y(t), T_w(t), T_h(t)]$$

¹R. Girshick (2013), Rich Feature Hierarchies



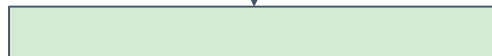
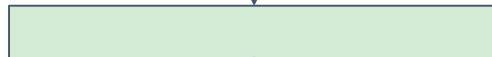
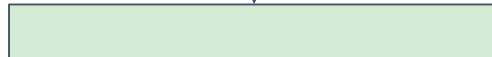
Method

$$B_i = [x_i, y_i, w_i, h_i]$$



$$\mathbf{B} = \{B_{-n+1}, B_{-n+2}, \dots, B_0\}$$

Input layer (size=4n)



Output layer (size=4*(p+2))

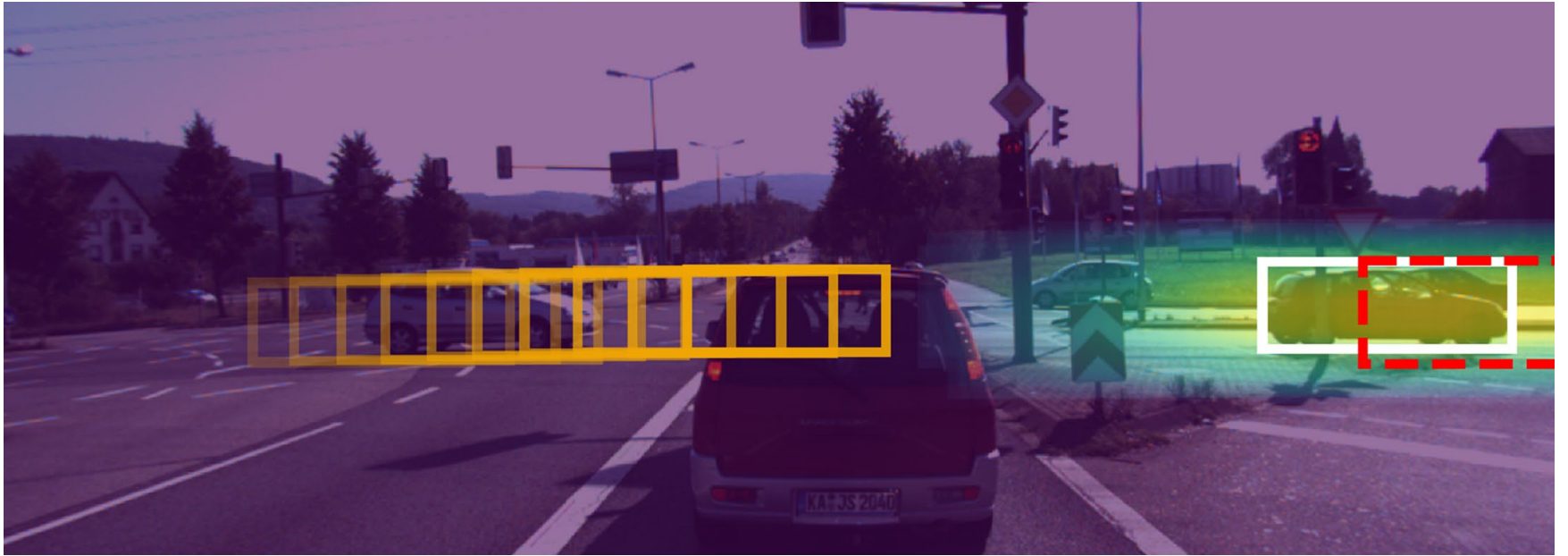
$$\theta_{\mathbf{B}} = \{\theta_{\mathbf{B}}^x, \theta_{\mathbf{B}}^y, \theta_{\mathbf{B}}^w, \theta_{\mathbf{B}}^h\}$$

$$\theta_{\sigma} = \{\theta_{\sigma}^x, \theta_{\sigma}^y, \theta_{\sigma}^w, \theta_{\sigma}^h\}$$

- Build polynomial from coefficients:

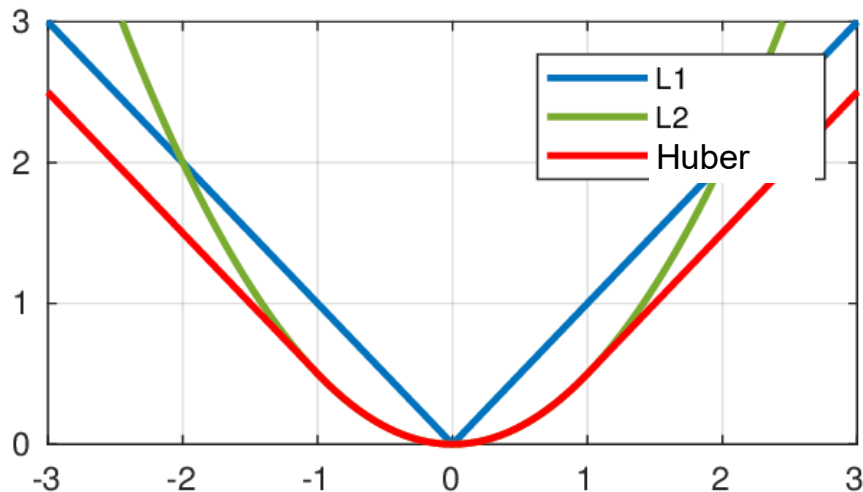
$$T_d(t; \theta_B^d) = \sum_{i=1}^p \theta_B^{d(i)} t^i.$$

$$\sigma_d(t; \theta_{\sigma}^d) = |\theta_{\sigma}^{d(1)} t| + |\theta_{\sigma}^{d(0)}|$$



Training for Confidence

- Formulating a Huber distribution



- Used for bounding box regression¹

Huber loss:

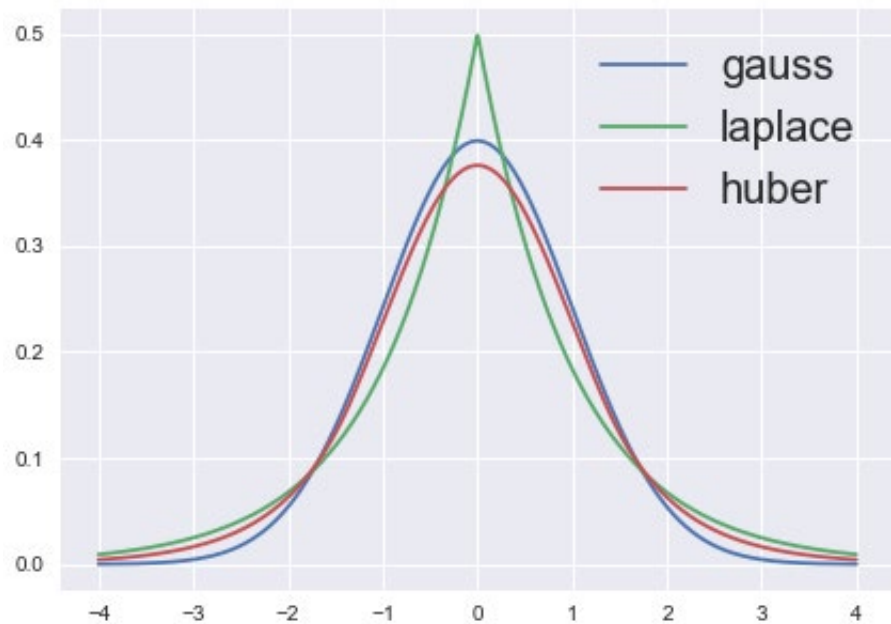
$$H(\hat{x}, x) = \begin{cases} \frac{1}{2} (\hat{x} - x)^2 & \text{if } |\hat{x} - x| < \tau \\ \tau |\hat{x} - x| - \frac{1}{2} \tau^2 & \text{otherwise,} \end{cases}$$

¹R. Girshick (2015), Fast R-CNN



Training for Confidence

- Formulating a Huber distribution



Gaussian pdf:

$$f(x | \mu, \sigma^2) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

Laplace pdf:

$$f(x | \mu, b) = \frac{1}{2b} \exp\left(-\frac{|x - \mu|}{b}\right)$$

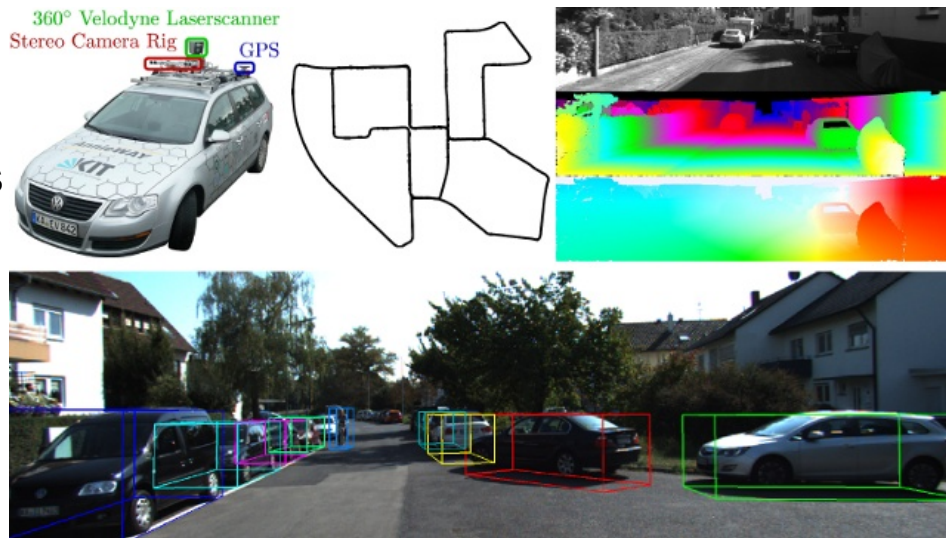
Huber pdf:

$$p(\hat{x}|x, \sigma) = \begin{cases} \frac{1}{c} \exp\left(-\frac{(\hat{x}-x)^2}{2\sigma^2}\right) & \text{if } |\hat{x} - x| < \tau \\ \frac{1}{c} \exp\left(-\frac{\tau}{\sigma^2}|\hat{x} - x| + \frac{\tau^2}{2\sigma^2}\right) & \text{otherwise,} \end{cases}$$



Experiments: Dataset

- KITTI “Raw” dataset
 - 38 videos of various scenes
- Sample creation:
 - Isolate 20 continuous frames for tracked objects
 - Use first 10 as ‘prior’ input
 - Next 10 frames are targets



Experiments: Evaluating the mean

		All					Hard				
Loss	Func.	DE		ADE	IoU		DE		ADE	IoU	
		+0.5s	+1.0s		+0.5s	+1.0s	+0.5s	+1.0s		+0.5s	+1.0s
-	constant	32.06	72.15	36.98	0.498	0.339	44.23	102.40	51.62	0.326	0.128
-	linear	14.61	39.51	17.95	0.663	0.464	23.14	63.27	28.56	0.492	0.219
L1	$p = 6$	12.81	29.05	14.78	0.697	0.564	17.06	38.06	19.56	0.607	0.475
L2	$p = 6$	15.13	37.43	18.12	0.671	0.521	20.90	51.97	25.02	0.563	0.394
Huber	$p = 6$	12.58	29.18	14.72	0.708	0.584	16.18	36.76	18.76	0.622	0.488
Huber	RNN	14.01	31.37	16.12	0.686	0.570	19.62	44.63	22.71	0.577	0.442

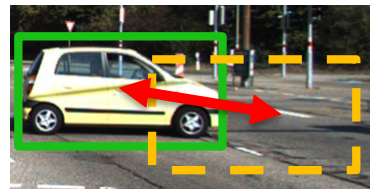
Metrics:

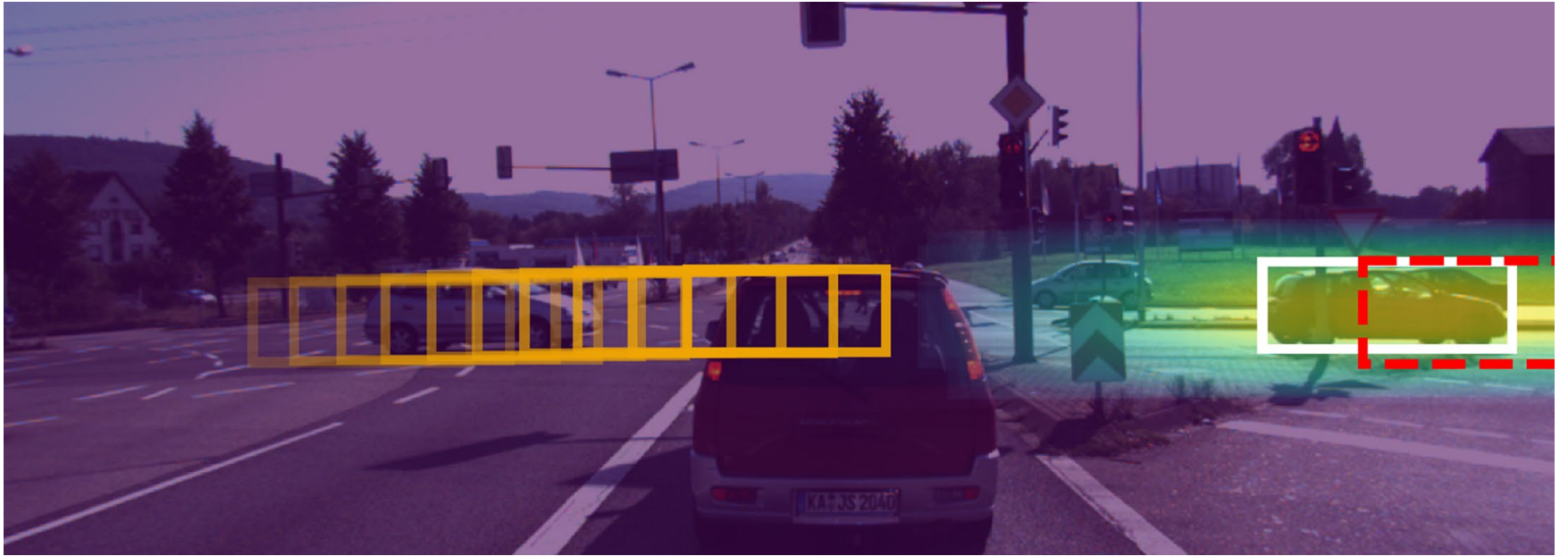
- Intersection over Union (IoU):



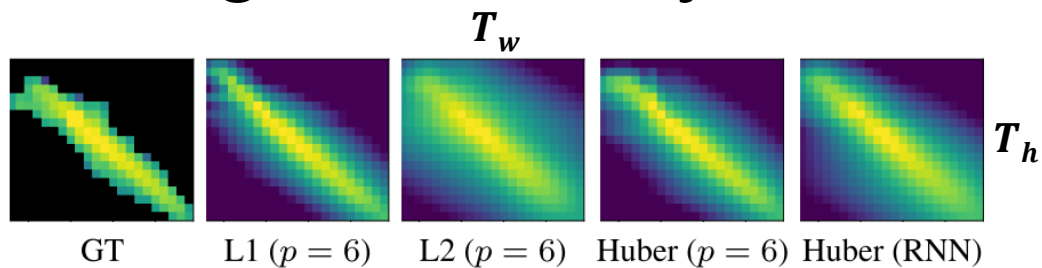
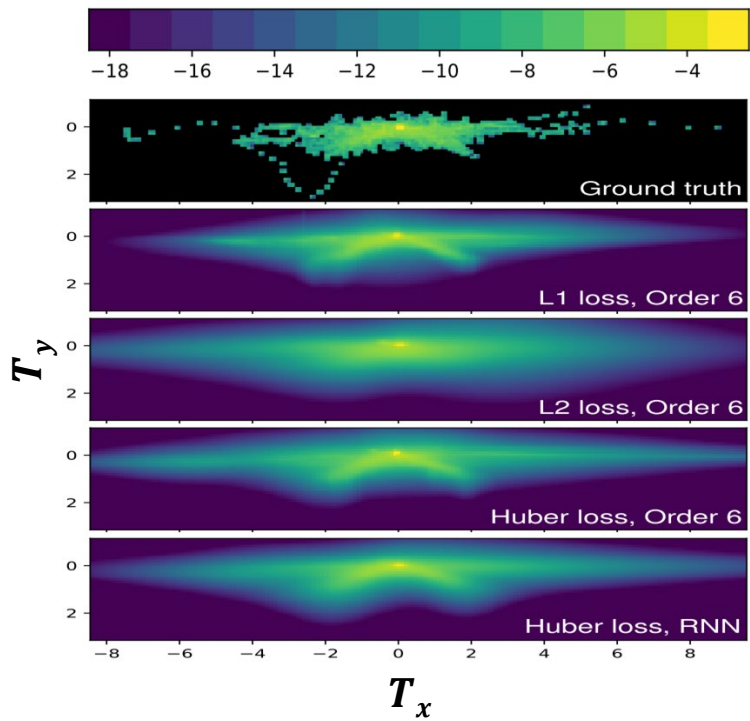
$$\frac{|A \cap B|}{|A \cup B|}$$

- Displacement Error (DE):





Experiments: Evaluating uncertainty



Config.	L1	L2	Huber	Huber (RNN)
$\mathcal{H}^2(\mathcal{T}, \hat{\mathcal{T}})$	0.568	0.607	0.562	0.562

Bin entire test set

Metric:

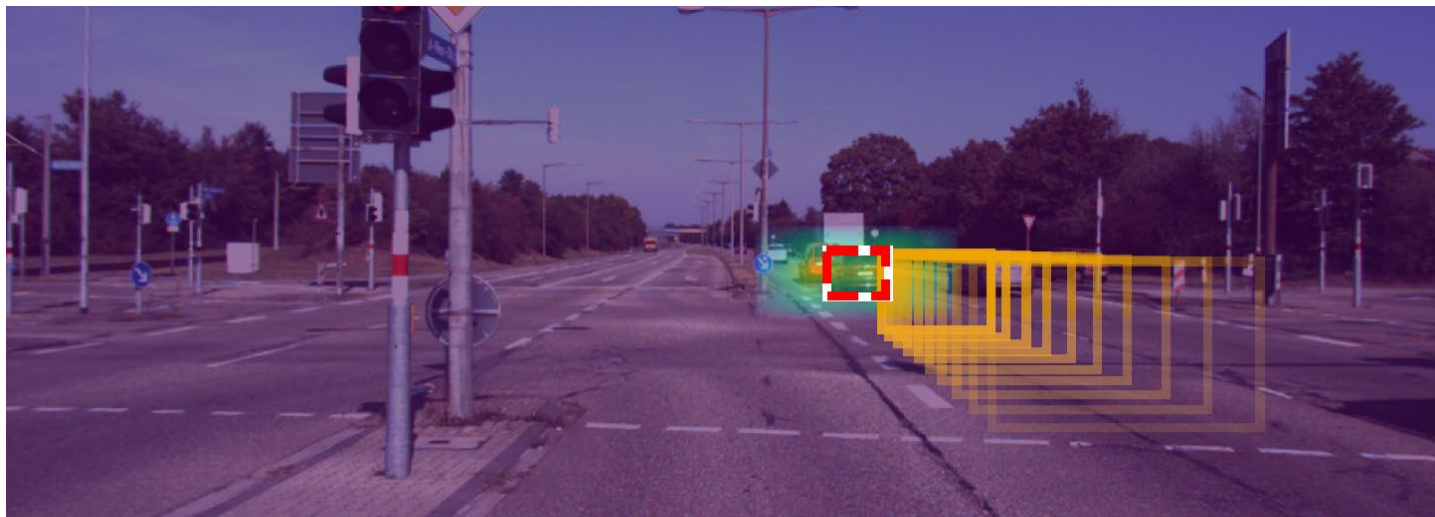
- Squared Hellinger Distance:

$$\mathcal{H}^2(\mathcal{T}, \hat{\mathcal{T}}) = \frac{1}{2} \|\sqrt{\mathcal{T}} - \sqrt{\hat{\mathcal{T}}}\|_2^2$$

Future Work

$$\sigma(t) = [\sigma_x(t), \sigma_y(t), \sigma_w(t), \sigma_h(t)]$$

- Model uncertainty as a joint distribution
- Integrate with object tracking



Thank you!

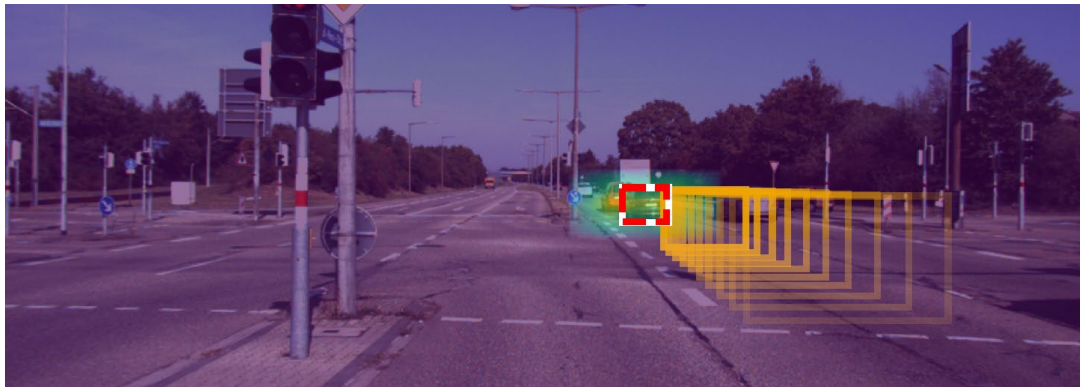
Questions?



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June 16-20, 2019



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